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### **The Affine Closure of $T^*(\mathrm{SL}_n/U)$**

We show that the affine closure  $\overline{T^*(\mathrm{SL}_n/U)}$  has symplectic singularities, in the sense of Beauville. In the special case  $n = 3$ , we show that the affine closure  $\overline{T^*(\mathrm{SL}_3/U)}$  is isomorphic to the closure  $\overline{\mathcal{O}_{\min}}$  of the minimal nilpotent orbit  $\mathcal{O}_{\min}$  in  $\mathfrak{so}_8$ . Moreover, the quasi-classical Gelfand-Graev action of the Weyl group  $W$  on  $\overline{T^*(\mathrm{SL}_3/U)}$  can be identified with the restriction to  $\overline{\mathcal{O}_{\min}}$  of E. Cartan's triality action on  $\mathfrak{so}_8$ .

**Keywords:** Symplectic singularities, triality action.

**MSC:** 20G05, 17B10, 14M15.